

III. 1) 2) 3) Part (1) : Medians Of Triangle

III Mechanism (1) : Median

Definition

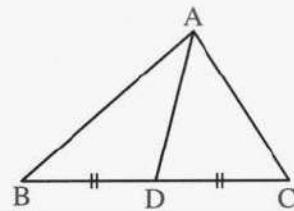
The median of the triangle is the line segment drawn from any vertex of the triangle vertices to the midpoint of the opposite side of this vertex.

For example :

In the opposite figure :

\because D is the midpoint of \overline{BC}

$\therefore \overline{AD}$ is the median of $\triangle ABC$



III Mechanism (2) : Point of Concurrency

Theorem (2)

The point of concurrence of the medians of the triangle divides each median in the ratio of 1 : 2 from its base.

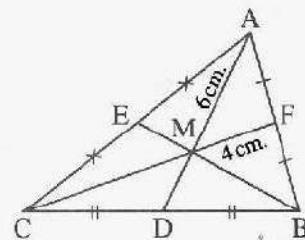
For example :

In the opposite figure :

In $\triangle ABC$, M is the point of intersection of its medians , then:

1 $MD = \frac{1}{2} AM$ IF $AM = 6 \text{ cm.}$, then $MD = 3 \text{ cm.}$

2 $CM = 2 FM$ IF $FM = 4 \text{ cm.}$, then $CM = 8 \text{ cm.}$



III Mechanism (3) : Median - Right-Angled Triangle :

Theorem (3)

In the right-angled triangle , the length of the median from the vertex of the right angle equals half the length of the hypotenuse.

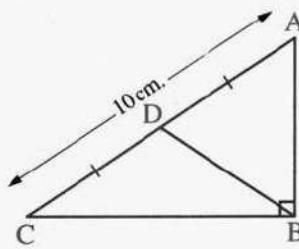
For example :

In the opposite figure :

$\triangle ABC$ is a right-angled triangle at B ,

D is the midpoint of \overline{AC} and $AC = 10 \text{ cm.}$,

then $DB = 5 \text{ cm.}$



Mechanism (3) Median – Right angle is right angle

The converse of theorem (3)

If the length of the median drawn from a vertex of a triangle equals half the length of the opposite side to this vertex, then the angle at this vertex is right.

For example :

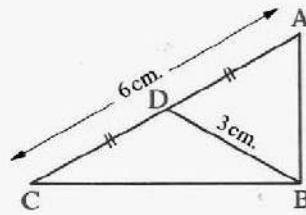
In the opposite figure :

If \overline{BD} is a median in $\triangle ABC$,

$BD = 3 \text{ cm.}$ and $AC = 6 \text{ cm.}$,

then $m(\angle ABC) = 90^\circ$

“because : $BD = \frac{1}{2} AC$ ”



Mechanism (5) Median – Right – 30 - 60

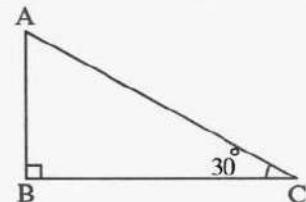
Corollary

The length of the side opposite to the angle of measure 30° in the right-angled triangle equals half the length of the hypotenuse.

In the opposite figure :

If $\triangle ABC$ is a right-angled at B and

$m(\angle C) = 30^\circ$, then $AB = \frac{1}{2} AC$



For example :

If $AC = 20 \text{ cm.}$, then $AB = 10 \text{ cm.}$

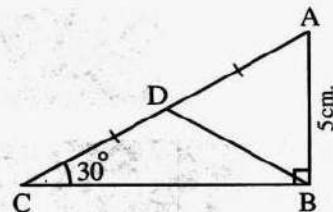
Examples on Part (1) : Medians of Triangle 10

① In the opposite figure :

$m(\angle B) = 90^\circ$ and $m(\angle C) = 30^\circ$

, $AB = 5 \text{ cm.}$

Find the length of : \overline{AC} and \overline{BD}



Solution

In $\triangle ABC$

$\because m(\angle B) = 90^\circ$

$\therefore m(\angle C) = 30^\circ$

$\therefore AC = 2 AB = 2 \times 5 = 10 \text{ cm}$

(First Req.)

$\because D$ is a midpoint of \overline{AC}

$\therefore \overline{BD}$ is a median

$\therefore BD = \frac{1}{2} AC = \frac{1}{2} \times 10 = 5 \text{ cm}$

(Second Req.)

② In the opposite figure :

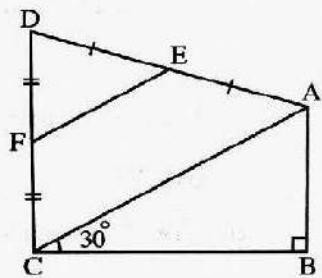
$$m(\angle B) = 90^\circ$$

$$, m(\angle ACB) = 30^\circ$$

, E is the midpoint of \overline{AD}

, F is the midpoint of \overline{CD}

Prove that : $AB = EF$



Solution

In $\triangle ABC$

$$\because m(\angle B) = 90^\circ$$

$$\because m(\angle C) = 30^\circ$$

$$\therefore BD = \frac{1}{2} AC \quad \dots \dots \dots (1)$$

In $\triangle ADC$

$\because E$ is a midpoint of \overline{AD}

$\because F$ is a midpoint of \overline{DC}

$$\therefore EF = \frac{1}{2} AC \quad \dots \dots \dots (2)$$

From (1) and (2)

$$\therefore AB = EF$$

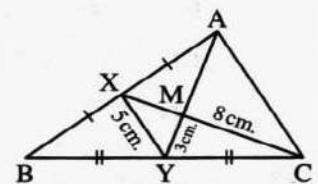
③ In the opposite figure :

ABC is a triangle , X is the midpoint of \overline{AB}

, Y is the midpoint of \overline{BC} , $\overline{XC} \cap \overline{AY} = \{M\}$

, $XY = 5$ cm. , $CM = 8$ cm. , $YM = 3$ cm.

Find the perimeter of : $\triangle MAC$



Solution

In $\triangle ABC$

$\because Y$ is a midpoint of \overline{BC}

$\because X$ is a midpoint of \overline{AB}

$$\therefore AC = 2 \times XY = 2 \times 5 = 10 \text{ cm}$$

$\because Y$ is a midpoint of \overline{BC}

$\therefore \overline{AY}$ is a median in $\triangle ABC$

$\because X$ is a midpoint of \overline{AB}

$\therefore \overline{CX}$ is a median in $\triangle ABC$

$\therefore M$ is the intersection point of medians in $\triangle ABC$

$$\therefore AM = 2 \times MY = 2 \times 3 = 6 \text{ cm}$$

The perimeter of $\triangle MAC = 6 + 8 + 10 = 24 \text{ cm}$

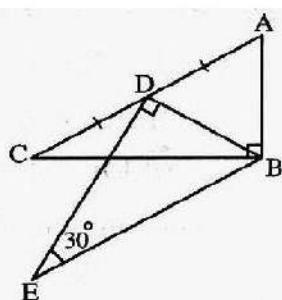
④ In the opposite figure :

$$m(\angle ABC) = m(\angle BDE) = 90^\circ$$

$$, m(\angle E) = 30^\circ$$

, D is the midpoint of \overline{AC}

Prove that : $AC = BE$



Solution

In $\triangle ABC$

$$\because m(\angle B) = 90^\circ$$

$\therefore D$ is a midpoint of \overline{AC}

$\therefore \overline{BD}$ is a median

$$\therefore BD = \frac{1}{2} AC \quad \dots \dots \dots (1)$$

In ΔDBE

$$\because m(\angle BDE) = 90^\circ$$

$$\therefore m(\angle E) = 30^\circ$$

$$\therefore BD = \frac{1}{2} BE \dots \dots \dots (2)$$

From (1) and (2)

$$\therefore AC = BE$$

(5) In the opposite figure :

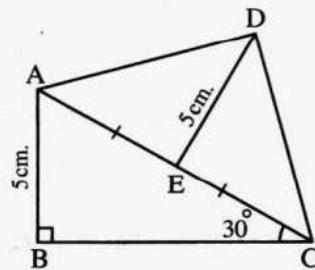
ABC is a right-angled triangle at B

$$, m(\angle ACB) = 30^\circ, AB = 5 \text{ cm.}$$

, E is the midpoint of \overline{AC}

$$\text{If } DE = 5 \text{ cm.}$$

Prove that : $m(\angle ADC) = 90^\circ$



Solution

In ΔABC

$$\because m(\angle B) = 90^\circ$$

$$\therefore m(\angle BCA) = 30^\circ$$

$$\therefore AB = \frac{1}{2} AC$$

$$\therefore AB = 5 \text{ cm}$$

$$AC = 5 \times 2 = 10 \text{ cm}$$

In ΔADC

$\because E$ is a midpoint of \overline{AC}

$\therefore \overline{ED}$ is a median

$$\therefore DE = 5 \text{ cm}$$

$$\therefore DE = \frac{1}{2} AC$$

$$\therefore m(\angle ADC) = 90^\circ$$

III (1) (2) Part (2) : Isosceles Triangle

III Mechanism (6) : Isosceles Triangle

Theorem (1)

The base angles of the isosceles triangle are congruent.

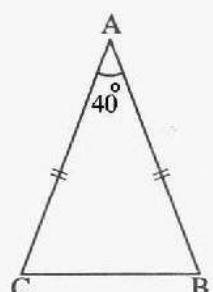
For example :

In the opposite figure :

If ABC is a triangle in which :

$$AB = AC, m(\angle A) = 40^\circ,$$

$$\text{then } m(\angle B) = m(\angle C) = \frac{180^\circ - 40^\circ}{2} = 70^\circ$$



III Mechanism (7) : Isosceles Triangle Equilateral

Corollary

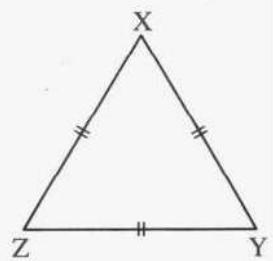
If the triangle is equilateral , then it is equiangular where each angle measure is 60°

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For example :

In the opposite figure :

If $\triangle XYZ$ is a triangle in which $XY = YZ = ZX$,
then $m(\angle X) = m(\angle Y) = m(\angle Z) = 60^\circ$



(ii) Mechanism (8) : To prove it is isosceles triangle

Theorem (2)

If two angles of a triangle are congruent, then the two sides opposite to these two angles are congruent and the triangle is isosceles.

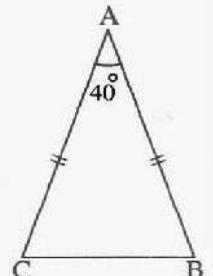
For example :

In the opposite figure :

If $\triangle ABC$ is a triangle in which :

$AB = AC$, $m(\angle A) = 40^\circ$,

then $m(\angle B) = m(\angle C) = \frac{180^\circ - 40^\circ}{2} = 70^\circ$



(iii) Mechanism (9) : Equilateral triangle

Corollary

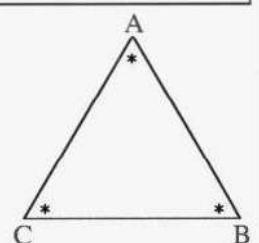
If the angles of a triangle are congruent, then the triangle is equilateral.

For example :

If $\triangle ABC$ is a triangle in which :

$\angle A \equiv \angle B \equiv \angle C$, then $AB = BC = CA$

i.e. $\triangle ABC$ is an equilateral triangle.



(iv) Mechanism (10) : Isosceles Equilateral triangle

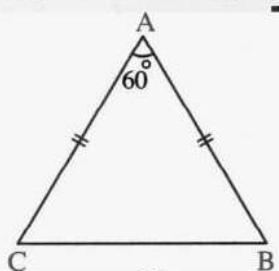
The isosceles triangle in which the measure of one of its angles $= 60^\circ$ is an equilateral triangle.

In the opposite figure :

If $AB = AC$ and $m(\angle A) = 60^\circ$

, then : $m(\angle B) = m(\angle C) = \frac{180^\circ - 60^\circ}{2} = 60^\circ$

$\therefore \triangle ABC$ is an equilateral triangle.



• In the opposite figure :

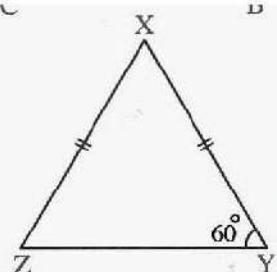
If $XY = XZ$

and $m(\angle Y) = 60^\circ$

, then $m(\angle Z) = 60^\circ$

, $m(\angle X) = 180^\circ - (60^\circ + 60^\circ) = 60^\circ$

$\therefore \triangle XYZ$ is an equilateral triangle.



(1) Mechanism (13) : Isosceles Triangle - Median

Corollary (1)

The median of an isosceles triangle from the vertex angle bisects it and is perpendicular to the base.

In the opposite figure :

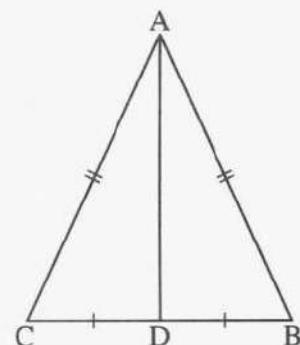
ABC is a triangle in which $AB = AC$ and

\overline{AD} is a median , then :

1 \overline{AD} bisects $\angle BAC$

i.e. $m(\angle BAD) = m(\angle CAD)$

2 $\overline{AD} \perp \overline{BC}$



(2) Mechanism (14) : Isosceles Triangle - Vertex Bisector

Corollary (2)

The bisector of the vertex angle of an isosceles triangle bisects the base and is perpendicular to it.

In the opposite figure :

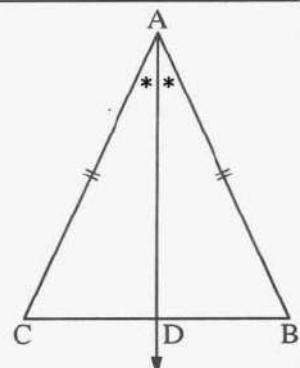
ABC is a triangle in which $AB = AC$ and

\overline{AD} bisects $\angle BAC$, then :

1 D is the midpoint of \overline{BC}

i.e. $BD = CD$

2 $\overline{AD} \perp \overline{BC}$



(3) Mechanism (13) : Isosceles Triangle - Perpendicular

Corollary (3)

The straight line drawn passing through the vertex angle of an isosceles triangle perpendicular to the base bisects each of the base and the vertex angle.

In the opposite figure :

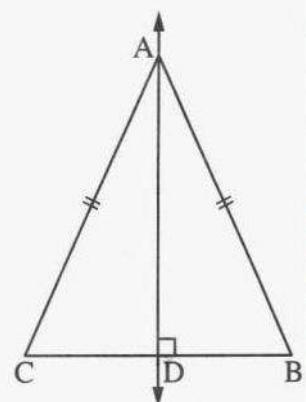
ABC is a triangle in which $AB = AC$ and

$\overleftrightarrow{AD} \perp \overline{BC}$, then

1 D is the midpoint of \overline{BC}

i.e. $BD = CD$

2 $m(\angle BAD) = m(\angle CAD)$



14 Mechanism (14) : Axis of symmetry of line segment (1)

Definition

The straight line perpendicular to a line segment at its middle is called the axis of symmetry for that line segment , in brief it is known as the axis of a line segment.

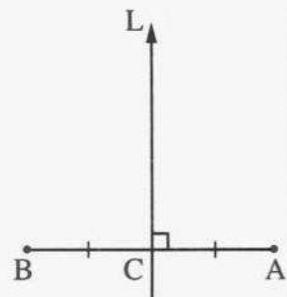
In the opposite figure :

If the straight line $L \perp \overline{AB}$ and $C \in L$ the straight

line L where C is the midpoint of \overline{AB} , then

the straight line L is called the

axis of \overline{AB}



15 Mechanism (15) : Axis of symmetry of line segment (2)

Property

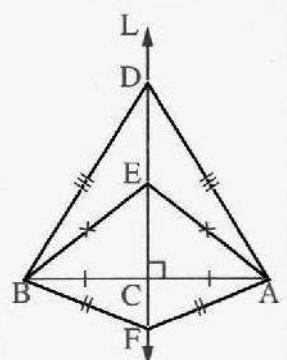
Any point on the axis of symmetry of a line segment is at equal distances from its terminals (end points).

In the opposite figure :

If the straight line L is the axis of \overline{AB} ,

$D \in L$, $E \in L$ and $F \in L$, then

$DA = DB$, $EA = EB$ and $FA = FB$

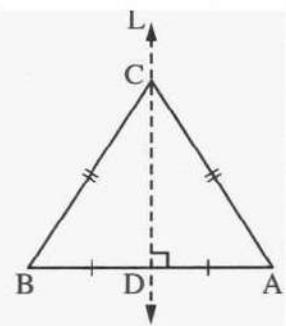


The converse of the previous property is true

i.e. If a point is at equal distances from the two terminals of a line segment , then this point lies on the axis of this line segment.

In the opposite figure :

If C is a point such
that $CA = CB$, then
the point C lies on the axis of \overline{AB}



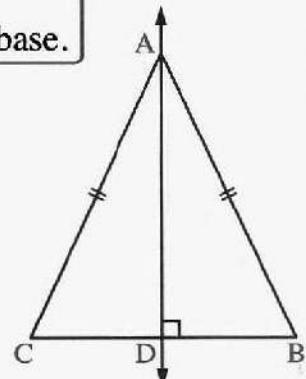
[16] Axes of symmetry of Isosceles Triangle

The isosceles triangle has one axis of symmetry.

It is the straight line drawn from the vertex angle perpendicular to its base.

For example :

If ABC is an isosceles triangle where
 $AB = AC$ and $\overrightarrow{AD} \perp \overline{BC}$, then :
 \overrightarrow{AD} is called the axis of symmetry
of the isosceles triangle ABC



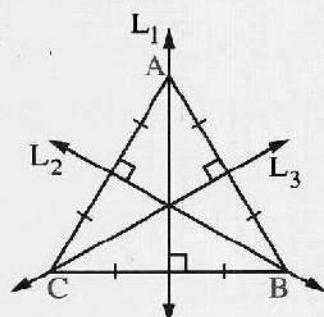
[17] Axes of Symmetry of Equilateral Triangle

1 The equilateral triangle has three axes of symmetry , they are the three
perpendiculars drawn from its vertices to the opposite sides.

In the opposite figure :

The straight lines L_1 , L_2 and L_3 are axes of
symmetry of the equilateral triangle ABC

2 The scalene triangle has no axes of symmetry.

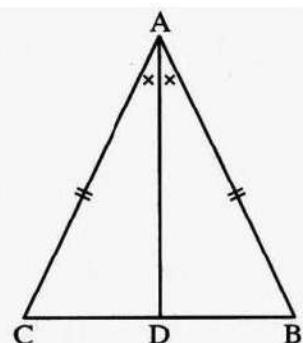


[18] Examples on Part (1) : Isosceles Triangle

① In the opposite figure :

In ΔABC :
 $AB = AC$, \overrightarrow{AD} bisects $\angle BAC$
and $BD = 3$ cm.

Prove that : $\overrightarrow{AD} \perp \overline{BC}$
, then find the length of : \overline{CB}



Solution

In $\triangle ABC$

$\because AB = AC$

$\therefore AD$ bisects $\angle BAC$

$\therefore AD \perp BC$ (First Req.)

$\therefore D$ is a midpoint of BC

$\therefore BD = 3 \text{ cm}$

$\therefore CD = BC = 3 \text{ cm}$

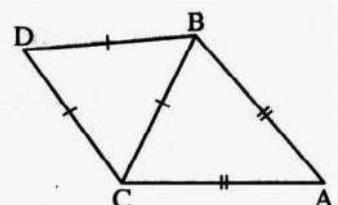
$\therefore CB = 3 \times 2 = 6 \text{ cm}$ (Second Req.)

② In the opposite figure :

$m(\angle A) = 50^\circ$, $AB = AC$

and $\triangle DBC$ is an equilateral.

Find : $m(\angle ABD)$



Solution

In $\triangle ABC$

$\because AB = AC$

$\therefore m(\angle A) = 50^\circ$

$\therefore m(\angle ABC) = m(\angle ACB)$

$\therefore m(\angle ABC) = (180 - 50) \div 2 = 65^\circ$

$\because \triangle DBC$ is an equilateral

$\therefore m(\angle DBC) = 60$

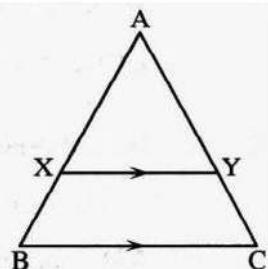
$\therefore m(\angle ABD) = 65 + 60 = 125^\circ$

③ In the opposite figure :

If $AB = AC$,

$\overline{XY} \parallel \overline{BC}$

Prove that : $\triangle AXY$ is an isosceles



Solution

In $\triangle ABC$

$\because AB = AC$

$\therefore m(\angle B) = m(\angle C)$

$\because XY \parallel BC$, AC & AB are transversals

$\therefore m(\angle B) = m(\angle AXY)$ Corresponding

$\therefore m(\angle C) = m(\angle AYX)$ Corresponding

In $\triangle AXY$

$\therefore m(\angle AXY) = m(\angle AYX)$

$\therefore AX = AY$

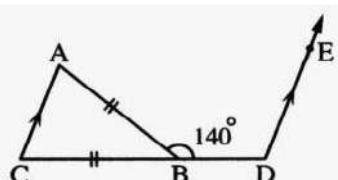
$\triangle AXY$ is an isosceles

④ In the opposite figure :

$\overline{CA} \parallel \overline{DE}$, $m(\angle ABD) = 140^\circ$

$AB = BC$

Find : $m(\angle EDB)$



Solution

In $\triangle ABC$

$\because AB = BC$

$$\therefore m \angle A = m \angle C$$

$$\therefore m \angle ABD = m \angle A + m \angle C \text{ (Exterior)}$$

$$\therefore m \angle ABD = 140^\circ$$

$$\therefore m \angle A = m \angle C = 140^\circ \div 2 = 70^\circ$$

$\because AC \parallel DE$, CD is a transversal

$$\therefore m(\angle C) + m(\angle D) = 180^\circ \text{ (Interior)}$$

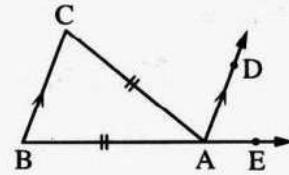
$$\therefore m(\angle D) = 180^\circ - 70^\circ = 110^\circ$$

⑤ In the opposite figure :

$$AB = AC,$$

$$\overrightarrow{AD} \parallel \overrightarrow{BC}$$

Prove that : \overrightarrow{AD} bisects $\angle CAE$



Solution

In $\triangle ABC$

$$\therefore AB = AC$$

$$\therefore m \angle B = m \angle C$$

$\therefore AC \parallel DE$, AB & AC are transversals

$$\therefore m \angle B = m \angle DAE \text{ (Corresponding)}$$

$$\therefore m \angle C = m \angle CAD \text{ (Alternate)}$$

$$\therefore m \angle DAE = m \angle CAD$$

AD bisects $m \angle CAE$

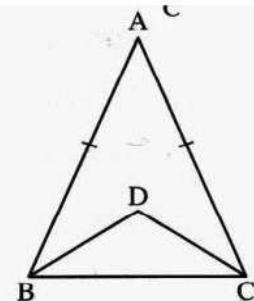
⑥ In the opposite figure :

ABC is a triangle in which $AB = AC$,

\overrightarrow{BD} bisects $\angle ABC$, \overrightarrow{CD} bisects $\angle ACB$

Prove that :

$\triangle DBC$ is an isosceles triangle.



Solution

In $\triangle ABC$

$$\therefore AB = AC$$

$$\therefore m \angle B = m \angle C$$

$\therefore BD$ bisects $m \angle ABC$

$\therefore CD$ bisects $m \angle ACB$

$$\therefore m \angle DBC = \frac{1}{2} m \angle ABC$$

$$\therefore m \angle DCB = \frac{1}{2} m \angle ACB$$

$$\therefore m \angle DBC = m \angle DCB$$

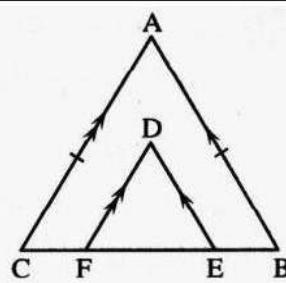
$\therefore \triangle DBC$ is an isosceles

⑦ In the opposite figure :

$AB = AC$, $\overrightarrow{DE} \parallel \overrightarrow{AB}$

, $\overrightarrow{DF} \parallel \overrightarrow{AC}$

Prove that : $DE = DF$



Solution

In $\triangle ABC$

$$\therefore AB = AC$$

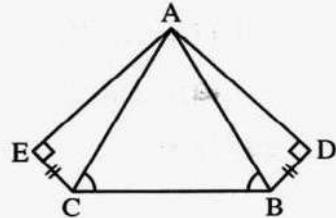
$\therefore m\angle B = m\angle C$
 $\because AC \parallel DF, CF$ is a transversal
 $\therefore AB \parallel DE, EB$ is a transversal
 $\therefore m\angle B = m\angle DEF$ (Corresponding)

$\therefore m\angle C = m\angle DFE$ (Corresponding)
 \because In $\triangle DEF$
 $\therefore m\angle DEF = m\angle DFE$
 $\therefore DE = DF$

⑧ In the opposite figure :

$BD = CE$
 $, m(\angle ABC) = m(\angle ACB)$
 $, m(\angle D) = m(\angle E) = 90^\circ$

Prove that : $m(\angle DAB) = m(\angle CAE)$



Solution

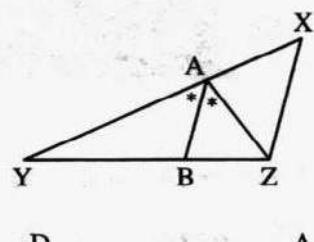
In $\triangle ABC$
 $\therefore m\angle ABC = m\angle ACB$
 $\therefore AB = AC$
 In $\triangle ABD, ACE$
 1) $AB = AC$

2) $BD = CE$
 3) $m\angle D = m\angle E = 90^\circ$
 $\therefore \triangle ABD \cong \triangle ACE$
 $\therefore m\angle DAB = m\angle CAE$

⑨ In the opposite figure :

\overrightarrow{AB} bisects angle YAZ
 $, \overrightarrow{AB} \parallel \overrightarrow{XZ}$

Prove that : $\triangle AXZ$ isosceles triangle.



Solution

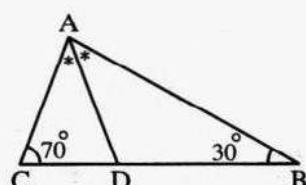
In $\triangle XYZ$
 $\therefore AB \parallel XZ, AZ$ is a transversal
 $\therefore m\angle BAZ = m\angle AZX$ (Alternate)
 $\therefore AB \parallel XZ, AX$ is a transversal
 $\therefore m\angle X = m\angle BAY$ (Corresponding)

$\because AB$ bisects angle YAZ
 $\therefore m\angle YAB = m\angle ZAB$
 $\therefore m\angle X = m\angle AZX$
 $\therefore AZ = AX$
 $\triangle XYZ$ is isosceles triangle

⑩ In the opposite figure :

\overrightarrow{AD} bisects $\angle BAC$
 $, m(\angle B) = 30^\circ$
 $, m(\angle C) = 70^\circ$

Prove that : $\triangle ADC$ is isosceles triangle.



Solution

In $\triangle ABC$

$$\therefore m\angle B = 30^\circ$$

$$\therefore m\angle C = 70^\circ$$

$$\therefore m\angle BAC = 180 - 30 - 70 = 80^\circ$$

\therefore AD bisects angle BAC

$$\therefore m\angle BAD = m\angle CAD = 80 \div 2 = 40^\circ$$

\therefore In $\triangle ADC$

$$\therefore m\angle ADC = 180 - 70 - 40 = 70^\circ$$

$$\therefore m\angle ADC = m\angle ACD = 70^\circ$$

$\therefore AD = AC$

$\triangle ADC$ is isosceles triangle

III Part (3) : Inequality

III Remember :

The measure of any exterior angle of a triangle is greater than the measure of any interior angle of the triangle except its adjacent angle.

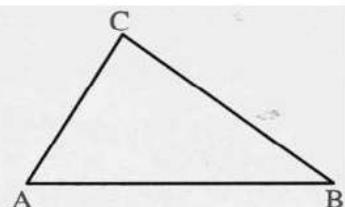
III Mechanism (18) : Comparing Angles :

Theorem

In a triangle , if two sides have unequal lengths , the longer is opposite to the angle of the greater measure.

i.e. In $\triangle ABC$:

If $AB > BC > AC$, then $m(\angle C) > m(\angle A) > m(\angle B)$
 $, m(\angle C) > 60^\circ$ and $m(\angle B) < 60^\circ$



III Mechanism (19) : Comparing Sides :

Theorem

In a triangle, if two angles are unequal in measure, then the greater angle in measure is opposite to a side greater in length than that opposite to the other angle.

III Mechanism (20) : Right-Angled Triangle :

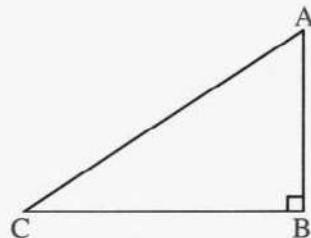
Corollary (1)

In the right-angled triangle , the hypotenuse is the longest side.

In the opposite figure :

If $\triangle ABC$ is right-angled at B , then $m(\angle B) > m(\angle A)$, $m(\angle B) > m(\angle C)$ because $\angle B$ is a right angle and each of $\angle A$ and $\angle C$ is acute so we find that :

$AC > BC$ and $AC > AB$ (according to the previous theorem).



Corollary (1)

In the obtuse-angled triangle , the side opposite to the obtuse angle is the longest side in the triangle.

Corollary (2) : Perpendicular Line Segments

Corollary (2)

The length of the perpendicular line segment drawn from a point outside a straight line to this line is shorter than any line segment drawn from this point to the given straight line.

In the opposite figure :

If $C \notin \overleftrightarrow{AB}$ and $D \in \overleftrightarrow{AB}$ such that

$\overline{CD} \perp \overline{AB}$, then

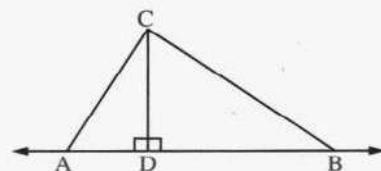
\overline{CB} is the hypotenuse in $\triangle CBD$ which is right-angled at D ,

\overline{CA} is the hypotenuse in $\triangle CDA$ which is right-angled at D and so on ...

According to corollary ① , we find that

$CB > CD$, $CA > CD$ and so on ...

i.e. $CD < CB$ and $CD < CA$



Definition

The distance between any point and a given straight line is the length of the perpendicular line segment drawn from this point to the given line.

Corollary (2) : Triangle Inequality

In any triangle , the sum of the lengths of any two sides is greater than the length of the third side.

مختصر توجيه الرياضيات لـ عاول إلؤول

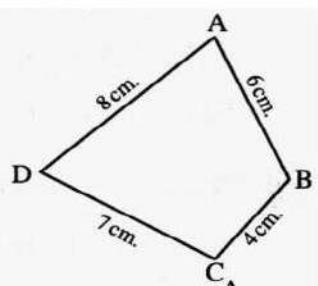
30. Problems of Part (C) : Inequality

① In the opposite figure :

ABCD is a quadrilateral where $AD = 8 \text{ cm.}$,

$AB = 6 \text{ cm.}$, $CB = 4 \text{ cm.}$ and $DC = 7 \text{ cm.}$

Prove that : $m(\angle \text{BAD}) < m(\angle \text{BCD})$

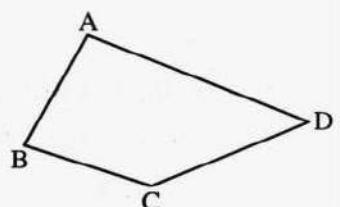


② In the opposite figure :

$AB < AD$, $BC < CD$

Prove that :

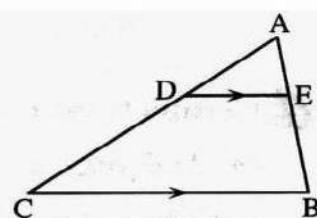
$m(\angle \text{ABC}) > m(\angle \text{ADC})$



③ In the opposite figure :

$\triangle \text{ABC}$ in which : $AC > AB$, $\overline{DE} \parallel \overline{CB}$

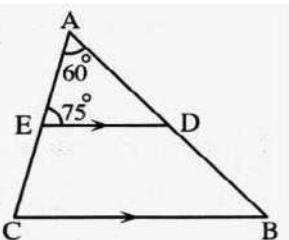
Prove that : $AD > AE$



④ In the opposite figure :

$\overline{ED} \parallel \overline{BC}$, $m(\angle \text{A}) = 60^\circ$

and $m(\angle \text{AED}) = 75^\circ$

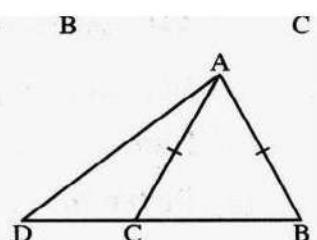


⑤ In the opposite figure :

If : $AB = AC$

Prove that :

$m(\angle \text{B}) > m(\angle \text{D})$

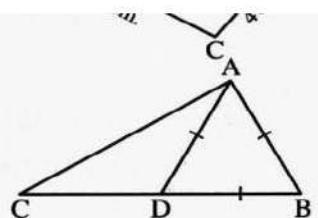


⑥ In the opposite figure :

$\triangle \text{ABC}$ is a triangle , $D \in \overline{BC}$

, $AB = AD = BD$

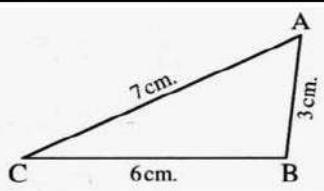
Prove that : $AC > AD$



⑦ In the opposite figure :

Arrange the angles of $\triangle \text{ABC}$

descendingly due to their measures

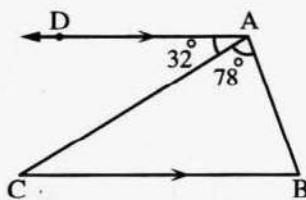


8 In the opposite figure :

$\overrightarrow{AD} \parallel \overrightarrow{BC}$, $m(\angle BAC) = 78^\circ$

, $m(\angle CAD) = 32^\circ$

Prove that : $AC > AB$



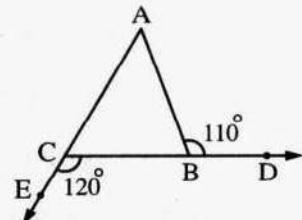
9 In the opposite figure :

ABC is a triangle , $D \in \overrightarrow{CB}$

, $E \in \overrightarrow{AC}$, $m(\angle ABD) = 110^\circ$

, $m(\angle BCE) = 120^\circ$

Prove that : $AB > BC$



10 In the opposite figure :

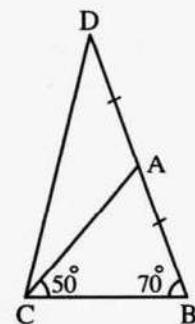
A is the midpoint of \overline{BD}

, $m(\angle ABC) = 70^\circ$

, $m(\angle ACB) = 50^\circ$

Prove that :

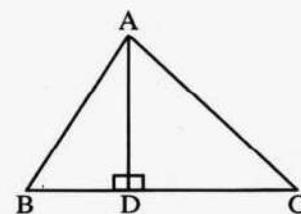
$m(\angle D) > m(\angle DCA)$



11 In the opposite figure :

Prove that :

$AC + AB > 2 AD$



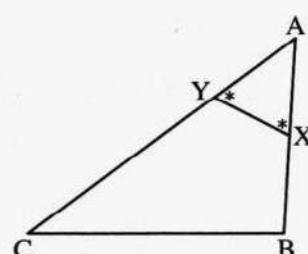
12 In the opposite figure :

ABC is a triangle in which $AC > AB$

, $X \in \overrightarrow{AB}$, $Y \in \overrightarrow{AC}$

where $m(\angle AXY) = m(\angle AYX)$

Prove that : $YC > XB$

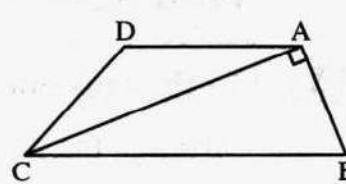


13 In the opposite figure :

$\overrightarrow{AC} \perp \overrightarrow{AB}$

, $\angle ADC$ is obtuse angle.

Prove that : $CB > DC$



Geom.

1-Complete

1. in the parallelogram , each two opposite sides are ,.....
2. in the //gram , each two consecutive angles are
3. the //gram whose diagonals are perpendicular is called
4. the parallelogram whose diagonals are equal in length and perpendicular is called
5. the rhombus whose diagonals are equal in length is called
6. the rectangle whose diagonals are perpendicular is called
7. ABCD is a //gram in which $m(\angle B) = \dots \circ$
8. the two diagonals of the square are ,
9. ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 140 \circ$
10. ABCD is a rectangle in which $m(\angle A) = 5x - 10$, then $x = \dots$

2-Complete

1. the medians of the triangle intersect at
2. the no. of medians in the right angled triangle is
3. the length of the median from the vertex of the right angle in the right angled $\Delta = \dots$
4. the length of the hypotenuse in thirty and sixty triangle = the length of the side opposite the angle whose measure is $30 \circ$
5. the line segment drawn between the two midpoints of two sides in a triangle is And its length =

1- complete:-

- 1- in the isosceles Δ if the measure of one of the two base angles 65° then the measure of its vertex angle =
- 2- in the isosceles Δ if the vertex angle = 50° then the measure of one of the two base angles =
- 3- if ABC is right angled Δ at A , $AB = AC$ then $m(\angle B) = \dots$
- 4- in ΔXYZ if $XY = XZ$, then the exterior angle at the vertex Z is
- 5- in ΔXYZ if $XY = YZ = ZX$, then $m(\angle X) = \dots^\circ$

2-Complete

- 1- if two angles in the triangle are congruent then the two sides opposite these two angles are and the triangle is
- 2- If the three angles in the triangle are congruent then the triangle is
- 3- If the isosceles Δ has angle = 45° , then the Δ is
- 4- In ΔABC if $AC = CB$ and $m(\angle C) = m(\angle A)$, then $m(\angle B) = \dots^\circ$
- 5- ABC is Δ $m(\angle A) = 30^\circ$, $m(\angle B) : m(\angle C) = 1 : 4$ then ΔABC is

1-Complete

- 1- the straight line drawn from the vertex of the isosceles Δ perpendicular to the base is called
- 2- the median of the isosceles Δ drawn from the vertex
- 3- The bisector of the vertex angle of the isosceles Δ
- 4- The st. line drawn from the vertex of an isosceles $\Delta \perp$ its base
- 5- Any point \in the axis of the line segment is from its two terminals
- 6- If $C \in$ the axis of symmetry of AB then $= AC$
- 7- The triangle whose angles are congruent has axes of symmetry
- 8- In ΔABC if $m(\angle A) = m(\angle B) \neq 60^\circ$ then the no. of axes of symmetry of triangle ABC is
- 9- If the length of each sides in the triangle $= \frac{1}{3}$ the perimeter of triangle then the no. of axes of symmetry of triangle is
- 10-If $ABCD$ is a rhombus then the axis of symmetry of AC is

2-Complete

- 1) The smallest angle of triangle (in measure) is opposite to
- 2) The longest side in the right angle triangle is
- 3) If triangle ABC $m(\angle A) = 50^\circ$ $m(\angle B) = 30^\circ$
- 4) If in triangle ABC $m(\angle A) = m(\angle B) + m(\angle C)$ then the longest side in the triangle is
- 5) in the triangle ABC if $m(\angle B) > m(\angle C)$ then $<$

[1] Complete :

- 1) The smallest angle of triangle (in measure) is opposite to
- 2) The longest side in right angled Δ is
- 3) The shortest distance between a given point and a given straight line is
.....
- 4) In ΔABC , $m(\angle C) = 120^\circ$ then its longest side is
- 5) In ΔABC , if $m(\angle A) = m(\angle B) + m(\angle C)$ then the longest side in the triangle
is

2-Complete

- 1) The lengths of side in Δ the sum of lengths of two other sides .
- 2) If the length of two sides in isosceles triangle are 7 cm , 4 cm then the length of the
third side =
- 3) A triangle has one axis of symmetry the lengths of two sides in it are 4 cm , 8 cm then
its perimeter =
- 4) In ΔABC if $AB = 3$ cm , $BC = 5$ cm , $AC = X$ cm then $X \in$

Revision on geometry

Unit 4

1) Medians of triangle

1- complete:-

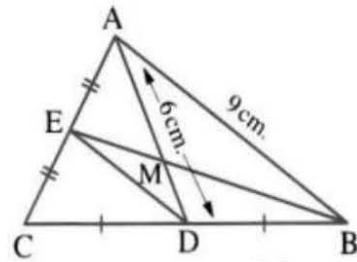
1. the medians of the triangle intersect at
2. the no. of medians in the right angled triangle is
3. the length of the median from the vertex of the right angle in the right angled Δ =
4. the length of the hypotenuse in thirty and sixty triangle = the length of the side opposite the angle whose measure is 30°
5. the line segment drawn between the two midpoints of two sides in a triangle is And its length =



In the opposite figure :

ABC is a triangle in which D is the midpoint of \overline{BC} , E is the midpoint of \overline{AC} and $\overline{AD} \cap \overline{BE} = \{M\}$

If $AD = 6$ cm. and $AB = BE = 9$ cm. , calculate the perimeter of ΔMDE

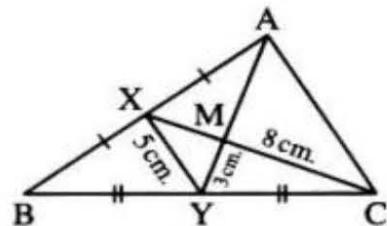


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In the opposite figure :

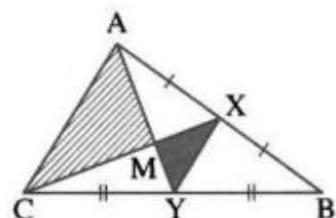
ABC is a triangle , X is the midpoint of \overline{AB} , Y is the midpoint of \overline{BC} , $\overline{XC} \cap \overline{AY} = \{M\}$, $XY = 5 \text{ cm.}$, $CM = 8 \text{ cm.}$, $YM = 3 \text{ cm.}$

Find the perimeter of : ΔMAC



In the opposite figure :

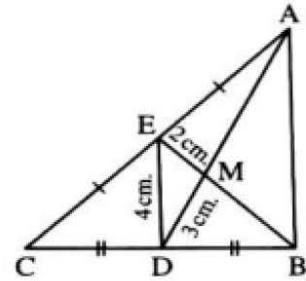
ABC is a triangle , X is the midpoint of \overline{AB} , Y is the midpoint of \overline{BC} , $XY = 5 \text{ cm.}$ and $\overline{XC} \cap \overline{AY} = \{M\}$ where $CM = 8 \text{ cm.}$, $YM = 3 \text{ cm.}$ **Find :**



1 The perimeter of ΔMXY

2 The perimeter of ΔMAC

Find perimeter of ΔAMB



In the opposite figure :

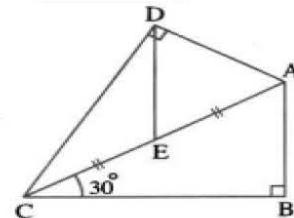
$m(\angle ABC) = m(\angle ADC) = 90^\circ$,

$m(\angle ACB) = 30^\circ$ and

E is the midpoint of \overline{AC}

Prove that : $AB = DE$

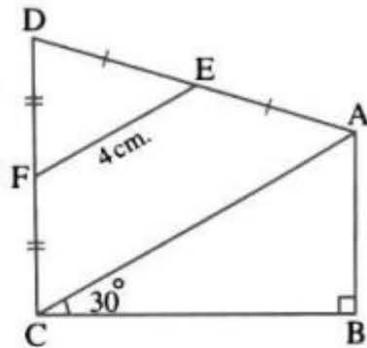
Solution



ABCD is a quadrilateral in which $m(\angle B) = 90^\circ$,
 E is the midpoint of \overline{AD} , F is the midpoint of \overline{CD}
 $m(\angle ACB) = 30^\circ$ and $EF = 4 \text{ cm}$.

Find by proof the length of : \overline{AB}

Solution

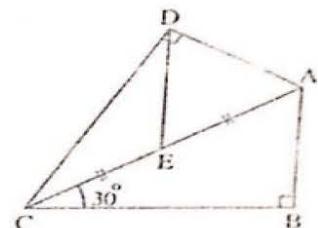


1- In the opposite figure:

$m(\angle ABC) = m(\angle ADC) = 90^\circ$,
 $m(\angle ACB) = 30^\circ$ and

E is the midpoint of \overline{AC}

Prove that: $AB = DE$



[1] Complete:

- 1 In the right-angled triangle the length of the median from the vertex of the right angle equal the length of the hypotenuse.
- 2 In the right-angled triangle , the length of the median from the vertex of the right angle equals
- 3 If the length of the median drawn from a vertex of a triangle equals half the length of the opposite side to this vertex in length , then
- 4 The length of the side opposite to the angle of measure 30° in the right-angled triangle equals the length of the hypotenuse.
- 5 The length of side opposite to the angle whose measure = 30° in the right-angled triangle =
- 6 The length of the hypotenuse on the right-angled triangle equals the length of a side opposite to the angle of measure 30°
- 7 In ΔLMN : If $m(\angle L) = 30^\circ$, $m(\angle N) = 60^\circ$, $NM = 4$ cm. , then $LN = \dots$ cm.
- 8 If ABC is a right-angled triangle at B , $AB = 6$ cm. , $BC = 8$ cm. , if \overline{BD} is a median of triangle ABC , then $BD = \dots$ cm.
- 9 In ΔABC , $m(\angle C) = 60^\circ$, $m(\angle B) = 90^\circ$, $AC = 8$ cm. , then $BC = \dots$ cm.

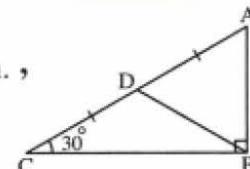


In the opposite figure :

$m(\angle B) = 90^\circ$, $m(\angle C) = 30^\circ$, \overline{BD} is a median , $AB = 4$ cm. ,

Complete :

$AC = \dots$ cm. , $BD = \dots$ cm. , $AD = \dots$ cm.



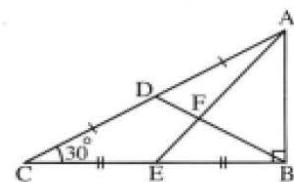
In the opposite figure :

ΔABC in which $m(\angle B) = 90^\circ$, $AC = 10$ cm. ,

$m(\angle C) = 30^\circ$, $EC = EB$, $AD = DC$

Find with proof : ① The perimeter of ΔABD

② The length of \overline{DF}



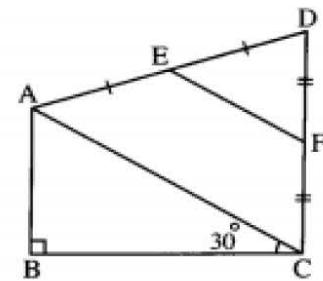
In the opposite figure :

$$m(\angle B) = 90^\circ ,$$

$$m(\angle ACB) = 30^\circ ,$$

E , F are midpoints of \overline{AD} , \overline{DC}

Prove that : $AB = EF$



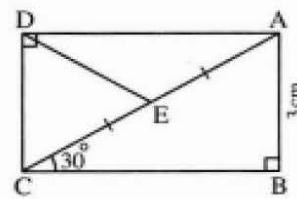
In the opposite figure :

$$m(\angle ABC) = m(\angle ADC) = 90^\circ ,$$

$m(\angle ACB) = 30^\circ$, and \overline{DE} is a median of $\triangle ADC$,

If $AB = 3$ cm.

Find : The length of \overline{DE}



Isosceles triangle

[1] Complete:

- 1 The two base angles in an isosceles triangle are
- 2 ΔABC , $AB = AC$, $m(\angle C) = 70^\circ$, then $m(\angle A) = \dots$
- 3 In the ΔABC : $AB = AC$, $m(\angle A) = 70^\circ$, then $m(\angle C) = \dots^\circ$
- 4 The ΔABC is an isosceles and right-angled triangle if $m(\angle B) = 90^\circ$, then $m(\angle A) = m(\angle C) = \dots^\circ$
- 5 In ΔABC , if $AB = AC$ and $m(\angle A) = 80^\circ$, then $m(\angle B) = m(\angle \dots) = \dots^\circ$
- 6 In ΔABC : if $AB = AC$, $m(\angle B) = 60^\circ$, then the triangle is an
- 7 In ΔABC : If $AB = AC$ and $m(\angle A) = 2 m(\angle C)$, then $m(\angle B) = \dots^\circ$
- 8 The length of side opposite to the angle whose measure = 30° in the right-angled triangle =

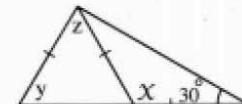


In the opposite figure complete :

$$x = \dots^\circ ,$$

$$y = \dots^\circ ,$$

$$z = \dots^\circ$$

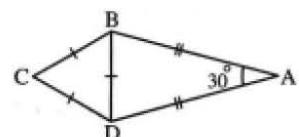


In the opposite figure :

$$AB = AD , m(\angle A) = 30^\circ ,$$

$$CB = BD = CD$$

Find : $m(\angle CBA)$

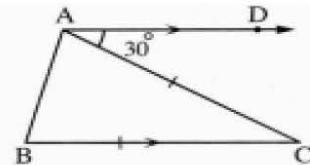


In the opposite figure :

ABC is a triangle in which : $AC = BC$,

$\overline{AD} \parallel \overline{BC}$, $m(\angle DAC) = 30^\circ$

Find : $m(\angle ABC)$

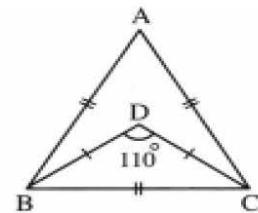


In the opposite figure :

ABC is an equilateral triangle ,

$DB = DC$, $m(\angle D) = 110^\circ$

Find with proof : $m(\angle DBC)$ and $m(\angle DBA)$



Converse of theorem of isosceles triangle

[1] Complete:

- 1 If angles of any triangle are equal in measures , then the triangle is
- 2 If the angles of a triangle are congruent , then the triangle is
- 3 The measure of the exterior angle of equilateral triangle =°
- 4 If the measure of one of the angles of the right-angled triangle is 45° , then the triangle is
- 5 In an isosceles triangle , if any angle has a measure of 60° , the triangle is
- 6 In ΔABC if : $\overline{AB} \perp \overline{BC}$ and $AB = BC$, then $m(\angle A) =^\circ$



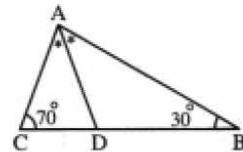
In the opposite figure :

\overrightarrow{AD} bisects $\angle BAC$

, $m(\angle B) = 30^\circ$

, $m(\angle C) = 70^\circ$

Prove that : ΔADC is isosceles triangle.



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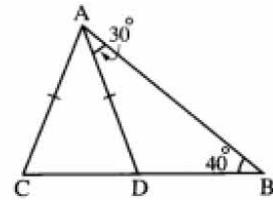
In the opposite figure :

$$AD = AC$$

$$, m(\angle DAB) = 30^\circ$$

$$, m(\angle ABD) = 40^\circ$$

Prove that : $AB = CB$



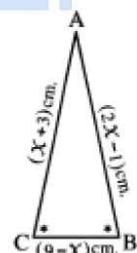
In the opposite figure :

$$m(\angle B) = m(\angle C), AB = (2x - 1) \text{ cm.}$$

$$AC = (x + 3) \text{ cm.}$$

$$, BC = (9 - x) \text{ cm.}$$

Find with proof the perimeter of ΔABC



Corollaries of isosceles triangle

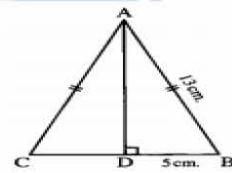
[1] Complete:

- 1 The ray drawn from the vertex of the isosceles triangle passing through the midpoint of the base is
- 2 The median of an isosceles triangle drawn from the vertex bisects and is perpendicular to
- 3 The bisector of the vertex angle of an isosceles triangle and
- 4 In ΔXYZ : If $XY = XZ$, $\overline{XL} \perp \overline{YZ}$, then \overline{XL} bisects each of and
- 5 The straight line perpendicular to the midpoint of a line segment is called
- 6 In the isosceles triangle if the measure of any angle is 60° , then the number of axis of symmetry
- 7 The number of axes of symmetry of the isosceles triangle equal
- 8 The number of symmetrical line in an scalene triangle =



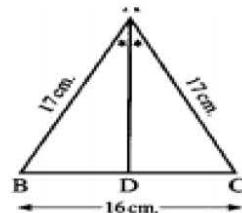
In the opposite figure :

In ΔABC , $AB = AC$,
 $\overline{AD} \perp \overline{BC}$,
 $AB = 13$ cm. and $BD = 5$ cm.
Find : 1 The length of \overline{BC}
2 The area of ΔABC



In the opposite figure :

\overline{AD} bisects $\angle BAC$,
 $AB = AC = 17$ cm. ,
and $BC = 16$ cm.
Prove that : $m(\angle ADB) = 90^\circ$,
then find the length of : \overline{AD} and the area of ΔABC



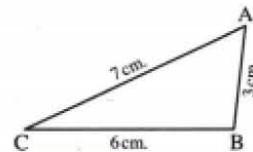
Inequality

1-Complete

- 1) The smallest angle of triangle (in measure) is opposite to
- 2) The longest side in the right angle triangle is
- 3) If triangle ABC $m(\angle A) = 50^\circ$ $m(\angle B) = 30^\circ$
- 4) If in triangle ABC $m(\angle A) = m(\angle B) + m(\angle C)$ then the longest side in the triangle is
- 5) in the triangle ABC if $m(\angle B) > m(\angle C)$ then <

In the opposite figure :

Arrange the angles of ΔABC
descendingly due to their measures

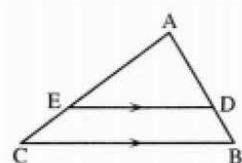


In the opposite figure :

$\overline{ED} \parallel \overline{BC}$,

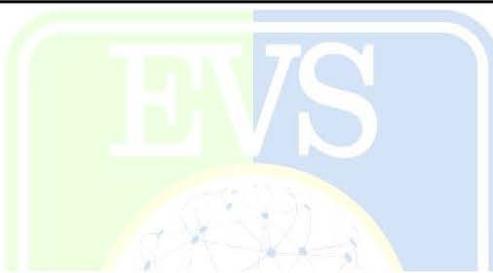
$AC > AB$

Prove that : $AE > AD$



[1] Choose the correct answer:

- | | | | | | |
|----------|---|----------------|----------------|----------------|----------------|
| 1 | In $\triangle ABC$, $AB > AC$, then $m(\angle C) \dots m(\angle B)$ | (a) $<$ | (b) $>$ | (c) $=$ | (d) \leq |
| 2 | In $\triangle ABC$ if $AB > AC$, then $m(\angle B) \dots m(\angle C)$ | (a) $>$ | (b) $<$ | (c) $=$ | (d) \geq |
| 3 | In $\triangle ABC$, $AB > AC$, $m(\angle C) = 70^\circ$, then $m(\angle B)$ may be | (a) 70° | (b) 50° | (c) 80° | (d) 75° |
| 4 | In $\triangle ABC$: If $BC > AB$, then $m(\angle A) \dots m(\angle C)$ | (a) $=$ | (b) $<$ | (c) \leq | (d) $>$ |
| 5 | In the triangle XYZ , if $XY > ZX$, then $m(\angle Y) \dots m(\angle Z)$ | (a) $>$ | (b) $<$ | (c) $=$ | (d) \geq |
| 6 | In $\triangle ABC$: $AB = AC$, $m(\angle B) = 65^\circ$, then : $AC \dots BC$ | (a) $<$ | (b) $>$ | (c) $=$ | (d) \leq |



In $\triangle ABC$ if : $AB = 14$ cm. , $BC = 6$ cm. and $AC = 10$ cm. Arrange the angles of $\triangle ABC$ ascendingly due to their measures.



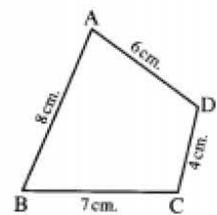
In the opposite figure :

$AB = 8$ cm. ,

$BC = 7$ cm. ,

$CD = 4$ cm. , $AD = 6$ cm.

Prove that : $m(\angle BCD) > m(\angle BAD)$



[1] Choose the correct answer:

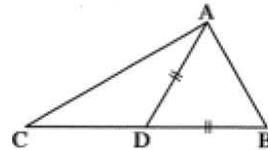
- | | | | | |
|----------|---|-------|-------|--------------|
| 1 | ΔXYZ , $m(\angle X) = 60^\circ$, $m(\angle Y) = 40^\circ$, then $XZ \dots XY$ | | | |
| | (a) < | (b) > | (c) = | (d) nothing. |
| 2 | ABC is a triangle in which : $m(\angle B) = 70^\circ$, $m(\angle C) = 50^\circ$, then $AC \dots AB$ | | | |
| | (a) > | (b) < | (c) = | (d) \equiv |
| 3 | In a triangle ABC : $m(\angle B) = 75^\circ$, $m(\angle C) = 50^\circ$, then $BC \dots AB$ | | | |
| | (a) < | (b) > | (c) = | (d) \equiv |
| 4 | ABC is a triangle in which : $m(\angle B) = 80^\circ$, $m(\angle C) = 50^\circ$, then $BC \dots AB$ | | | |
| | (a) > | (b) < | (c) = | (d) \equiv |
| 5 | If : $m(\angle A) = 50^\circ$ and $m(\angle B) = 60^\circ$ in triangle ABC then $AB \dots AC$ | | | |
| | (a) > | (b) < | (c) = | (d) \leq |



 In the opposite figure :

ABC is a triangle and $D \in \overline{BC}$ where $BD = AD$

Prove that : $BC > AC$

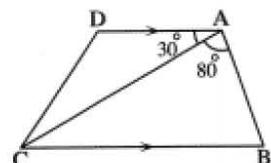


 In the opposite figure :

$\overrightarrow{AD} // \overrightarrow{BC}$, $m(\angle BAC) = 80^\circ$ and $m(\angle DAC) = 30^\circ$

Prove that :

$BC > AB$



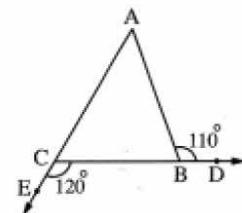
 In the opposite figure :

ABC is a triangle , $D \in \overrightarrow{CB}$,

$E \in \overrightarrow{AC}$, $m(\angle ABD) = 110^\circ$

and $m(\angle BCE) = 120^\circ$

Prove that : $AB > BC$

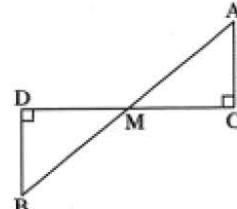


 In the opposite figure :

$\overline{AB} \cap \overline{CD} = \{M\}$, $\overline{AC} \perp \overline{CD}$ and $\overline{BD} \perp \overline{CD}$

Prove that :

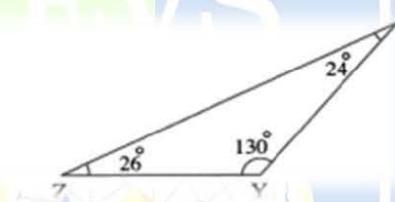
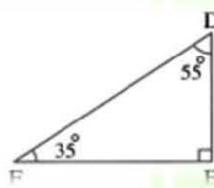
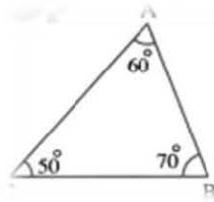
$AB > CD$



[1] Complete :

- 1) The lengths of side in Δ the sum of lengths of two other sides .
- 2) If the length of two sides in isosceles triangle are 7 cm , 4 cm then the length of the third side =
- 3) A triangle has one axis of symmetry the lengths of two sides in it are 4 cm , 8 cm then its perimeter =
- 4) In ΔABC if $AB = 3$ cm , $BC = 5$ cm , $AC = x$ cm then $x \in$

Arrange the lengths of sides of the following triangles ascending



Final Revision Geometry Prep2

[1] Complete:

- 1) The length of the median drawn from the vertex of the right angle in the right - angled triangle the length of the hypotenuse
- 2) The number of axes of symmetry of the equilateral triangle is
- 3) The medians of the triangle intersect at
- 4) The sum of lengths of any two sides in any triangle the length of the third side
- 5) the measure of an angle of the isosceles triangle is 100 , then the measure of one of the other angles =.....
- 6) The axis of symmetry of the line segment is
- 7) The two base angles of the isosceles triangle are
- 8) The measure of the exterior angle of the equilateral triangle =
- 9) If the lengths of two sides in the triangle are not equal, then the greater side in length is opposite to.....
- 10) The sum of measure of any two consecutive angles in the parallelogram =...
- 11) The median of an isosceles triangle drawn from the vertex bisects and is perpendicular to
- 12) The isosceles triangle has axis of symmetry.
- 13) The length of the side opposite the angle of measure 30 in the right-angled triangle the length of the hypotenuse.
- 14) The longest side in the right-angled triangle is
- 15) ABC is a triangle in which AB = AC , $m(\angle A) = 50$, then $m(\angle B)$
- 16) ABC is a triangle in which $AB > BC > AC$, then the smallest angle in measure of it is
- 17) The point of intersection of the medians of any triangle divides each of them with the ratio from the base.
- 18) If the point A \in the axis of symmetry of BC , then AB =
- 19) ABC is a triangle in which AB = 4 cm , BC = 5 cm. then AC $\in].....,$
- 20) If AD is a median in ABC , M is the point of intersection of the medians of it , then AD = AM
- 21) If the lengths of two sides in a triangle are not equal, then the greater side in length is opposite
- 22) The two base angles of the isosceles triangle are.....
- 23) If ABC is a right - angled at B and $AB = \frac{1}{2} AC$, then $m(\angle A)$
- 24) If the lengths of two sides in the isosceles triangle are 5 cm and 10 cm , then the length of the third side = Cm.
- 25) Each two opposite angles in the parallelogram are.....
- 26) The triangle which has no axis of symmetry istriangle.
- 27) If AD is a median of ABC , M is the point of intersection of the median of ABC , then AM= AD

- 28) In the isosceles triangle if the measure of one of the two base angle 50 , then the measure of the vertex angle
- 29) The axis of symmetry of a line segment is the straight line which is
- 30) In ΔABC , if $m(\angle B) = 70$ and $m(\angle C) = 50$, then : $AB \dots AC$
- 31) In the parallelogram , the two diagonals are
- 32) If x cm , 4 cm and 5 cm. are lengths of the sides of a triangle , then ... $x < \dots$
- 33) The longest side in the right-angled triangle is
- 34) The bisector of the vertex angle of the isosceles triangle is
- 35) Any point on the axis of symmetry of a line segment is
- 36) The length of the side opposite the angle whose measure 30 in the right – angled triangle equals
- 37) If ABC has one axes of symmetry and $m(\angle ABC) = 120$, then $m(\angle A) = \dots$
- 38) In ABC if $m(\angle A) = 30$ and $m(\angle B) = 90$, then $AC = \dots$
 $(BC \text{ or } 2 BC \text{ or } 2 AB \text{ or } BC) \square$
- 39) If ABC is right - angled at B , then $AB \dots AC$
- 40) If 3 cm and 7 cm are two lengths of two sides in a triangle , then the greatest integer representing the length of the third side is Cm
- 41) The length of the median drawn from the vertex of the right angle of the right-angled triangle equals
- 42) The perpendicular bisector of a line segment is called
- 43) The point of intersection of the medians of the triangle bisects each of them with the ratio : From the base
- 44) If the lengths of two sides of a triangle are not equal, then the greater side in length is opposite
- 45) If the length of the median of a triangle drawn from a vertex is equal to the half length of the opposite side , then the angle of this vertex is
- 46) If the lengths of two sides of an isosceles triangle are
11 cm and 5 cm , then the length of the third side is.....
- 47) The number of axes of symmetry of the triangle in which the measure of two angles are 60 and 70 equals
- 48) The length of the hypotenuse of the right-angled triangle = the length of the median drawn from the vertex of the right angle.
- 49) In ΔABC if $m(\angle B) - m(\angle A) > m(\angle C)$, then $AC \dots AB$
- 50) If the lengths of two sides of a triangle are not equal
, then the greater in length is opposite
- 51) The bisector of the vertex angle of the isosceles triangle
- 52) If the length of any side of a triangle = $\frac{1}{3}$ the perimeter of the triangle , then the number of axes of symmetry of the triangle is
- 53) If the lengths of two sides of a triangle are 5 cm and 7 cm , then the length of the third side] , [
- 54) In the parallelogram , the two diagonals
- 55) If ABC has one axis of symmetry and $m(\angle B) = 120$, then $m(\angle A) \dots$

- 56) The point of the intersection of the medians of the triangle divides each of them with ratio from the vertex.
- 57) In ΔABC , $AB \square + BC \square - AC > \dots$
- 58) The bisector of the vertex angle of the isosceles triangle
- 59) If in ΔABC : $AB = AC$ and $m(\angle A) = 2 m(\angle B)$, then $m(\angle C) \dots$
- 60) The isosceles triangle in which the measure of one of its angles is 60° , has axes of symmetry.
- 61) If the lengths of two sides of a triangle are not equal then the longer side is opposite an angle Then the measure of the angle opposite the other
- 62) An isosceles triangle, one of its base angles has measure 70° then the measure of the vertex angle is
- 63) An isosceles triangle the lengths of two sides of it are 4 cm and 9 cm then the length of the third side = cm.
- 64) In ΔXYZ : $m(\angle Y) = 110^\circ$, then the longer side is
- 65) In ΔABC : $m(\angle A) = 55^\circ$, $m(\angle B) = 70^\circ$, then the number of axes of symmetry of the triangle is
- 66) the point of intersection of the medians of the triangle divides each of them with the ratio $1 : 2$ from
- 67) The median which is drawn from the vertex of an isosceles triangle bisects and it is to the base.
- 68) ΔABC is right - angled at B, $AB = 3 \text{ cm}$, $BC = 4 \text{ cm}$ if BD is a median of ΔABC then $BD \dots \text{ cm}$.
- 69) ΔABC is right - angled at B then $AC \dots BC$
- 70) If $\Delta ABC \cong \Delta XYZ$, then $AC = \dots$
- 71) If the measure of one of the angles of an isosceles triangle is 60° then the triangle is
- 72) The bisector of the vertex angle of the isosceles triangle bisects the base and it is
- 73) If the measure of one angle of the two base angles of the isosceles triangle 75° , then the measure of the vertex angle
- 74) The measure of the exterior angle of the equilateral triangle =
- 75) If ΔABC is an obtuse - angled triangle at C then $AB \dots AC$
- 76) The perpendicular bisector of a line segment is called
- 77) In the parallelogram each two opposite sides are

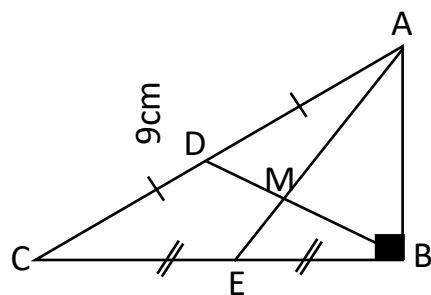
- 1) ΔABC is a triangle in which $m(\angle B) = 90^\circ$

$m(\angle C) = 30^\circ$, $AC = 9 \text{ cm}$

\overline{AE} , \overline{BD} are two medians

Intersecting at M, find the length

of \overline{BD} , \overline{BM} , \overline{AB}

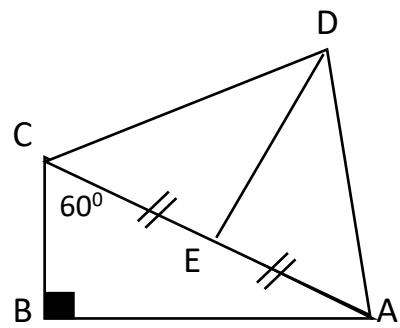


2) ABC is a right angled Δ at B,

$m(\angle ACB) = 60^\circ$, E is midpoint

of \overline{AC} and $DE = BC$

Prove that: $m(\angle ADC) = 90^\circ$



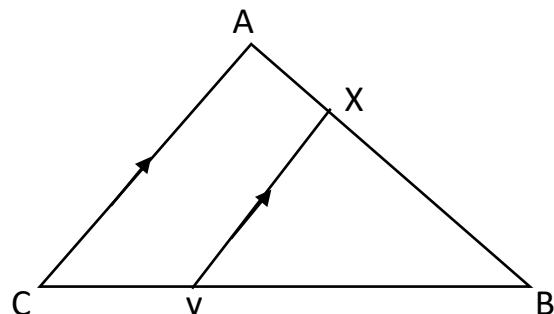
3) In the opposite figure:

$AB = BC$, $X \in \overline{AB}$ and $Y \in \overline{BC}$

Such that: $\overline{XY} \parallel \overline{AC}$

Prove that:

$m(\angle BXY) = m(\angle BYX)$

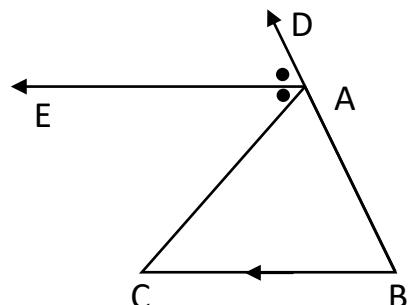


4) In the opposite figure:

$A \in \overrightarrow{BD}$, $\overrightarrow{AE} \parallel \overrightarrow{BC}$

and \overrightarrow{AE} bisects $\angle CAD$

Prove that: $AB = AC$

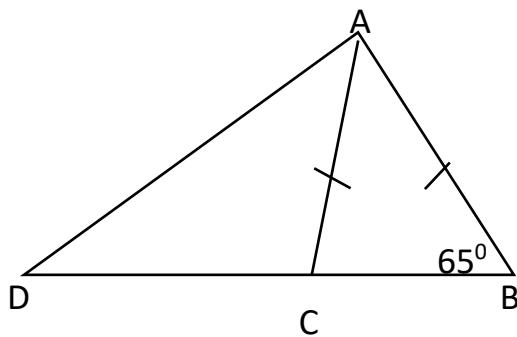


5) In the opposite figure:

$AB = AC = CD$ and $m(\angle B) = 65^\circ$

Find by proof:

$m(\angle BAD)$

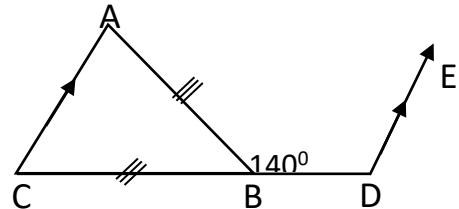


6) In the opposite figure:

$\overrightarrow{DE} \parallel \overrightarrow{AC}$, $AB = BC$

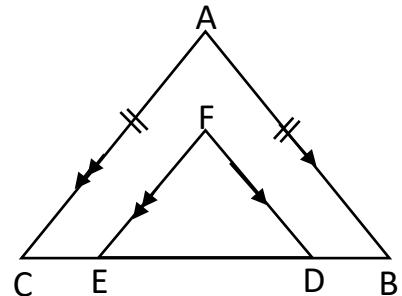
and $m(\angle ABD) = 140^\circ$

find $m(\angle EDB)$



7) $D \in \overline{BC}$, $E \in \overline{BC}$, $\overline{AB} \parallel \overline{FD}$ and $\overline{AC} \parallel \overline{FE}$ if $AB = AC$

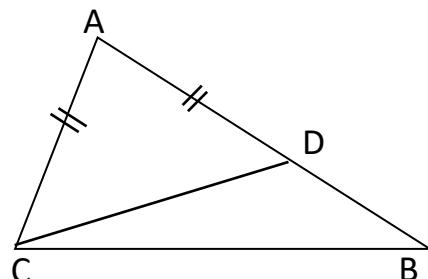
Prove that: FDE is an isosceles triangle.



8) In the opposite figure:

$D \in \overline{AB}$ where $AD = AC$

Prove that: $m(\angle ACB) > m(\angle B)$

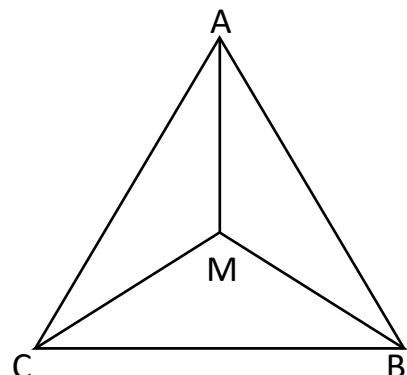


9) In the opposite figure:

ABC is a triangle in which M is

A point inside it, prove that:

$m(\angle AMC) > m(\angle ABC)$

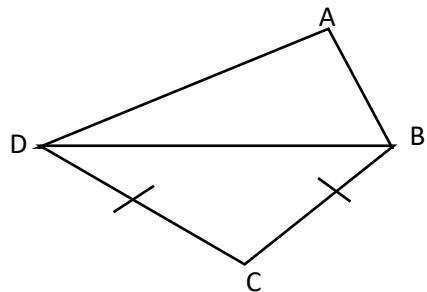


10) In the opposite figure:

$ABCD$ is a quadrilateral in which

$AD > AB$ and $BC = CD$

Prove that: $m(\angle ABC) > m(\angle ADC)$



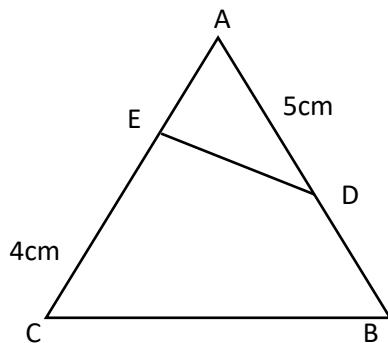
11) In the opposite figure:

ABC is a triangle in which

$AB = AC$ and $DB > DC$

Prove that:

$m(\angle ABD) > m(\angle ACD)$

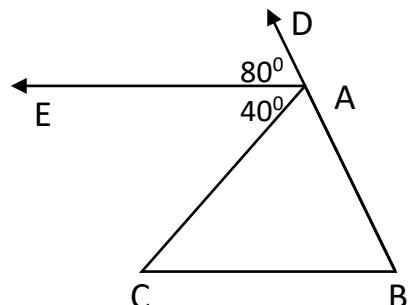


12) In the opposite figure:

$\overrightarrow{AE} \parallel \overrightarrow{BC}$, $m(\angle DAE) = 80^\circ$

and $m(\angle EAC) = 40^\circ$

Prove that: $AC > AB$

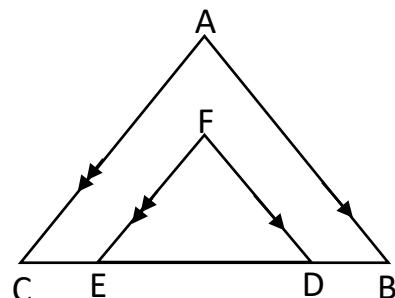


13) In the opposite figure:

$\overrightarrow{AB} \parallel \overrightarrow{DF}$, $\overrightarrow{AC} \parallel \overrightarrow{EF}$

$AC > AB$

Prove that: $FE > DF$

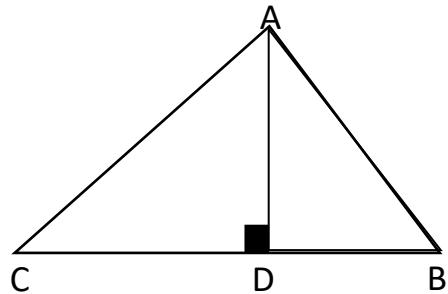


14) In the opposite figure:

ABC is a triangle in which

$$AC > AB, \overline{AD} \perp \overline{BC}$$

Prove that: $m(\angle BAD) < m(\angle CAD)$



15) In the opposite figure:

ABC is a triangle in which

$$AB = AC, D \in \overline{BC}$$

Prove that: $AB > AD$

